



**SCE594: Special Topics in Intelligent Automation & Robotics**  
**Assignment 5**

**Instructions:**

- This is a **graded** assignment of 5%.
- You can do the assignment either **individually** or in a **group of 2**.
- You can write on the pdf directly with a tablet & electronic pen **or** print the pdf and answer with an ink-pen.
- Good handwriting and neatness makes your work easier to read and understand and is highly recommended.
- Upload your solution as a **single compressed folder** on Blackboard by **11:59pm Thursday 30 April 2026 (end of the day)**. Include your MATLAB code with the pdf.
- If you do the assignment in a group of two, both members should upload the pdf file.
- Plagiarism will **not be tolerated** at all.

<b>Student 1 Name:</b>	
<b>Student 1 ID:</b>	

<b>Student 2 Name:</b>	
<b>Student 2 ID:</b>	



## 1. Introduction

- In this assignment you will study how to control the orientation of a rigid body in 3D space using a PD (proportional-derivative) controller directly on the rotation group  $SO(3)$ .
- The provided MATLAB script, `rigid_body_PD_control.m`, simulates the dynamics of a rigid body with a diagonal inertia matrix. The code applies different desired orientations over an 8-second window, switching to a new orientation every 2 seconds.

## 2. Given Code Explanation

Open `rigid_body_PD_control.m` in MATLAB. You will see these main sections:

### 1. Simulation Setup

- Time-step  $dt$ , total simulation time  $T$ , and number of steps  $steps$ .
- Inertia matrix  $inertia$ .
- Initial orientation  $R$  and angular velocity  $omega$ .
- Four different desired orientations  $RdSet$ , each selected for a 2-second interval.

### 2. Integration & Visualization

- A loop runs from  $i = 1$  to  $steps$ .
- At each time step, the code checks which desired orientation  $Rd$  should be active.
- It calls a **(placeholder) PD controller** function named `pd_controller` to compute the control torque  $\tau$ .
- The torque is then passed to an integrator `lie_poisson_midpt_solver` to update orientation and angular momentum.
- Plots of angular velocity and a 3D rigid body are updated in real time.

### 3. Utility Functions

- `lie_poisson_midpt_solver` for integrating orientation on  $SO(3)$ .
- `skew`, `skew_inv`, and `rodrigues` for matrix operations on rotations.

### 4. `pd_controller` (Placeholder)

- In this empty function you will add your controller as part of the assignment tasks below.

## 3. Assignment Requirements

- **Implement Two Different Geometric PD Controllers**

In the script, you will see a function:

```
function tau_k = pd_controller(R_k, w_k, Rd)
% PD controller for orientation on SO(3)
% R_k : Current orientation (3x3)
% w_k : Current angular velocity in body frame (3x1)
% Rd : Desired orientation (3x3)

% STUDENT TASK: Fill in TWO PD controllers
end
```



You must fill in the logic inside `pd_controller` to compute  $\tau_k$  based on the orientation error and angular velocity.

Implement two PD controllers: 1) a geometric one that computes the proportional term from the gradient of a function  $\Psi(R)$  as we did in class, 2) a standard PD controller using Euler angle parameterization.

You are free to try out other extra control approaches e.g. different  $\Psi(R)$  functions on  $SO(3)$ , feedback linearization or quaternion based ... etc.

- **Experiment with Gains**
  - Choose **at least two** different sets of  $(K_p, K_d)$  (or your chosen gain matrices) for **each** of your two PD approaches.
  - For each set, run the simulation and collect:
    1. The angular velocity plots vs. time ( $\omega_1, \omega_2, \omega_3$ ).
    2. The control torque  $\tau$  vs. time (plot *tauHistory* similarly or produce a separate figure to show how torque evolves).
- **Report in pdf format**
  - **Figures:** Submit plots for  $\omega(t)$  and  $\tau(t)$  for each of your two PD controller variants and for **at least two** gain settings each (total: 4 sets of plots).
  - **Discussion:** For each set of gains, comment on the comparison of the two (or more) approaches in terms of:
    - i. How does the body converge to the desired orientation.
    - ii. Whether there is overshoot or oscillation.
    - iii. The magnitude of the control torque.

#### 4. Assignment Deliverables:

You should turn in:

1. **Modified rigid\_body\_PD\_control.m**  
Ensure it contains your final code for `pd_controller` with both PD approaches. You can handle this in separate “if/else” statements or as two separate functions.
2. **Plots & Explanation**
  - A PDF with the requested plots ( $\omega$  vs. time,  $\tau$  vs. time) for each approach and each gain set.
  - A short write-up describing your findings, especially how changes to the gains affected convergence and torque demands.

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#### Hints:

- Remember that the code is already set to change orientations every 2 seconds. You should see how your controller transitions from one orientation to the next.
- If you see large transients or intense oscillations, consider tuning  $K_d$  and  $K_p$ .
- The desired rotation matrix  $R_d$  is not shown in the figure. You can modify the code to plot the axes of the desired frame if you wish.